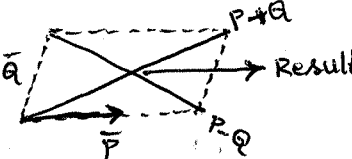


ECET-CIVIL-2022 - solutions (1)

51) $\rightarrow K.E = \frac{1}{2} m v^2 \rightarrow \text{Dimensions } [M^1 L^2 T^{-2}] \quad [2]$

54) $\rightarrow$ 1 mole gas volume $V = 22.4 \text{ litre}$
 $1 \text{ m}^3 = 1000 \text{ litre} \rightarrow V = \frac{22.4}{1000} \text{ m}^3$
 $V = 2.24 \times 10^{-2} \text{ m}^3 \quad [1]$

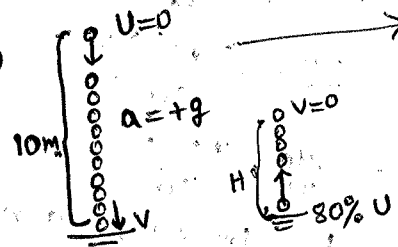
56) $\rightarrow$  The result is parallel to $\vec{P} \Rightarrow \text{Angle } 0^\circ \quad [4]$

57) $\rightarrow |\vec{A} \cdot \vec{B}| = 6 \rightarrow AB \cos \theta = 6 \quad [3]$
 $|\vec{A} \times \vec{B}| = 6\sqrt{3} \rightarrow AB \sin \theta = 6\sqrt{3}$
 $\Rightarrow \frac{\sin \theta}{\cos \theta} = \tan \theta = \frac{6\sqrt{3}}{6} \rightarrow \theta = \tan^{-1}(\sqrt{3}) = 60^\circ$

58) $\rightarrow P = Q = F$
 $\theta = 120^\circ$
 Result $R = \sqrt{P^2 + Q^2 + 2PQ \cos \theta} \quad [3]$
 $= \sqrt{F^2 + F^2 + 2FF \cos 120^\circ}$
 $= \sqrt{F^2 + F^2 + 2F^2(-\frac{1}{2})}$
 $R = \sqrt{2F^2 - F^2} = \sqrt{F^2} = F$

60) $\rightarrow \theta = 45^\circ$
 $R = H$
 $R = \frac{U^2 \sin 2\theta}{g} = \frac{U^2 \sin 90^\circ}{g} = \frac{U^2}{g} \quad [4]$
 $H = \frac{U^2 \sin^2 \theta}{2g} = \frac{U^2 \sin^2 45^\circ}{2g} = \frac{U^2}{4g}$
 $H = \frac{R}{4} \rightarrow R = 4H$

61) $\rightarrow U = 10 \text{ m/s}$
 $\theta = 60^\circ$
 $V_x = ?$
 $V_x = U \cos \theta$ is same in projectile. $[4]$
 $= 10 \cos 60^\circ = 5 \text{ m/s.}$

63)  $[2]$
 $V^2 - U^2 = 2as$
 $V^2 - 0 = 2g \times 10$
 $V^2 = 200$
 $V^2 - U^2 = 2as$
 $0 - (80\% U)^2 = -2gH$
 $H = \frac{80\% U^2}{2g}$
 $H = \frac{80}{100} \times \frac{200}{2 \times 10} = 8 \text{ metre.}$

(2)

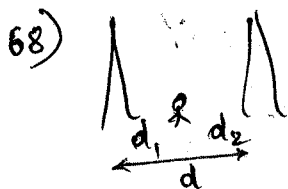
64) $\rightarrow m = 10 \text{ kg}$
 $m = 10 \text{ kg}$
 $v = 5 \text{ m/s}$
 $K.E = \frac{1}{2} m v^2 = \frac{1}{2} \times 10 \times 5^2 = 125 \text{ J}$ [2]

66) $\rightarrow T = 2\pi \sqrt{\frac{l}{g}} \rightarrow l = \frac{g T^2}{4\pi^2}$ [2]

$T = 2 \text{ sec}$ for Second's pendulum $\rightarrow$ constant
 $l \propto g$ $g \downarrow$ on moon $\Rightarrow l \downarrow$

67) $a = \omega^2 r = 31.4 \text{ m/s}^2$
 $v = r \omega = 10 \text{ m/s}$
 $T = ?$ [3]

$\frac{\omega^2 r}{r \omega} = \frac{31.4}{10}$
 $\omega = 3.14$
 $\frac{2\pi}{T} = 3.14$
 $T = \frac{2 \times 3.14}{3.14} = 2 \text{ sec.}$



$d = d_1 + d_2$, $c = \frac{2d}{\lambda}$, $c = \text{constant}$ [3]
 $= \frac{c t_1}{2} + \frac{c t_2}{2}$
 $= \frac{340 \times 1}{2} + \frac{340 \times 2}{2}$
 $= 170 + 340 = 510 \text{ m.}$

69) $n_1 = 256 \text{ Hz}$
 $n_2 = 258 \text{ Hz}$
 $T = ?$

Beat frequency $\Delta n = (n_1 - n_2)$ [2]
 $= 258 - 256$
 $\Delta n = 2 \text{ Hz}$
 $T = \frac{1}{\Delta n} = \frac{1}{2} = 0.5 \text{ seconds.}$

72) $m_1 \rightarrow 2m_1$
 $m_2 \rightarrow 2m_2$
 $d \rightarrow 2d$
 $F \rightarrow ?$

initial force $F_1 = \frac{\mu_0}{4\pi} \frac{m_1 m_2}{d^2}$ [2]

Now $F_2 = \frac{\mu_0}{4\pi} \times \frac{2m_1 \times 2m_2}{(2d)^2}$

$= \frac{\mu_0}{4\pi} \times \frac{4m_1 m_2}{4d^2}$

$F_2 = F_1$ Unchange (same)

73) $R = \frac{1}{2}$

(3)

$$73) \rightarrow R = \frac{\rho L}{A} = \frac{\rho L}{\pi r^2} = \frac{4 \rho L}{\pi D^2}$$

[3]

Now diameter is $\frac{D}{2} \rightarrow$ New Resistance is

$$\rightarrow \frac{4 \rho L}{\pi \left(\frac{D}{2}\right)^2} \rightarrow 4 \times \frac{4 \rho L}{\pi D^2} \rightarrow 4R$$

74) Under Bridge balancing condition

[1]

$$\frac{P}{Q} = \frac{R}{S} \rightarrow \frac{5}{15} = \frac{R+12}{60}$$

$$\rightarrow \frac{1}{3} = \frac{R+12}{60}$$

$$\rightarrow \frac{60}{3} = R+12 \rightarrow 20 = R+12$$

$$\rightarrow R = \underline{8 \Omega}$$