

52)

1) Moment of Inertia $I = m r^2 \rightarrow [M^1 L^2 T^0]$
 Moment of Force $\tau = F \times r \rightarrow [M^1 L^2 T^{-2}]$ } not equal. [1]

2) WORK $W = F \times s \rightarrow [M^1 L^2 T^{-2}]$
 Torque $\tau = F \times d \rightarrow [M^1 L^2 T^{-2}]$ } equal

3) Angular Momentum $L = m v r \rightarrow [M^1 L^2 T^{-1}]$
 Planck Constant $h = \frac{E}{\nu} \rightarrow [M^1 L^2 T^{-1}]$ } equal.

4) Impulse $I = F \times t \rightarrow [M^1 L^1 T^{-1}]$
 Momentum $P = m \times v \rightarrow [M^1 L^1 T^{-1}]$ } equal.

51)

Parsec is the unit of distance used in Astrology.
 1 parsec = 3.26 light years. [2]

53)

$P = F$
 $Q = 2F$
 $R = 2F$
 $\theta = ?$

$$R = \sqrt{P^2 + Q^2 + 2PQ \cos \theta}$$

$$2F = \sqrt{F^2 + 4F^2 + 4F^2 \cos \theta}$$

$$4F^2 = 5F^2 + 4F^2 \cos \theta \rightarrow \cos \theta = -\frac{1}{4} \rightarrow \theta = \cos^{-1}\left(-\frac{1}{4}\right)$$

[2]

54)

Co-planar $\rightarrow \det[A] = 0 \rightarrow \begin{vmatrix} 1 & -2 & 3 \\ x & 0 & 3 \\ 7 & 3 & -11 \end{vmatrix} = 0$

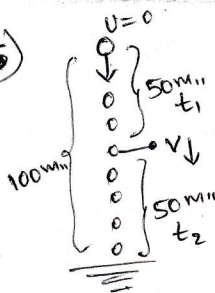
$$1(0-9) + 2(-11x-21) + 3(3x-0) = 0$$

$$-9 - 22x - 42 + 9x = 0 \rightarrow 13x = -51$$

$$x = -51/13$$

[2]

55)



In Free fall case velocity increases 9.8 m/sec per every sec. [2]

$V = \frac{d}{t}$ $V \uparrow$ so $t \downarrow$
 for 1st half distance (50m) $\rightarrow t_1$, V (high)
 2nd half " " $\rightarrow t_2$, V increase (very high)
 clearly $t_2 < t_1$ (or) $t_1 > t_2$

(OR)

$$U=0, S = Ut + \frac{1}{2}at^2, t = t_1 + t_2$$

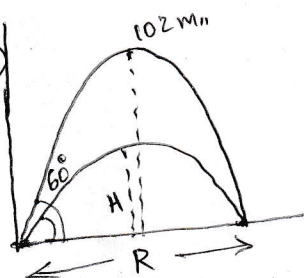
$$100 = \frac{1}{2}gt^2 \rightarrow t = \sqrt{20} = 4.47 \text{ sec.}$$

$$50 = \frac{1}{2}gt_1^2 \rightarrow t_1 = \sqrt{10} = 3.17 \text{ sec.}$$

$$t_2 = t - t_1 = 1.3 \text{ sec.}$$

} $t_1 > t_2$

56)



Range $R = \frac{U^2 \sin 2\theta}{g}$, $\sin 2(60^\circ) = \sqrt{3}/2$
 $\sin 2(30^\circ) = \sqrt{3}/2$ } same Range

So, angle for 2nd body is 30° .

$$\text{and } H = \frac{U^2 \sin^2 \theta}{g} \rightarrow 102 = \frac{U_1^2 \sin^2 60^\circ}{10} \rightarrow U_1^2 = \frac{1020}{3/4}$$

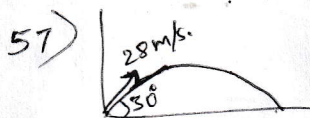
$$\rightarrow U_1^2 = 1360$$

and Same Ranges.

$$R = R \rightarrow \frac{U_1^2 \sin^2(60^\circ)}{g} = \frac{U_2^2 \sin^2(30^\circ)}{g} \rightarrow U_1^2 = U_2^2 \rightarrow U_1 = U_2$$

$\therefore$ 2nd Height with $\theta = 30^\circ$ is

$$H = \frac{U_2^2 \sin^2 \theta}{g} = \frac{1360 \times \sin^2 30^\circ}{10} = \frac{136}{4} = 34 \text{ metre}$$



$$T = \frac{2U \sin \theta}{g} = \frac{2 \times 28 \times \sin 30^\circ}{9.8} = \frac{28}{9.8} = 2.857$$

[1]

$$T = 2.9 \text{ sec}$$

58) $H = \frac{R}{2} \rightarrow \frac{U^2 \sin^2 \theta}{2g} = \frac{U^2 \sin 2\theta}{2g} \rightarrow \sin^2 \theta = 2 \sin \theta \cos \theta$

[4]

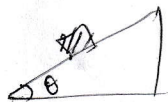
$$\rightarrow \tan \theta = 2 \rightarrow \theta = \tan^{-1}(2)$$

$$\rightarrow \sin \theta = \frac{2}{\sqrt{5}}, \cos \theta = \frac{1}{\sqrt{5}}$$

$$\therefore R = \frac{U^2 \sin 2\theta}{g} = \frac{U^2 \sin 2\theta}{g}$$

$$\therefore R = \frac{U^2 \sin 2\theta}{g} = \frac{U^2 \times 2 \sin \theta \cos \theta}{g} = \frac{2U^2 \times \frac{2}{\sqrt{5}} \times \frac{1}{\sqrt{5}}}{g} = \frac{4U^2}{5g}$$

59)



$$\mu = \frac{1}{\sqrt{3}} = \tan \theta \rightarrow \theta = \tan^{-1}\left(\frac{1}{\sqrt{3}}\right) = 30^\circ$$

[1]

60) In equilibrium $\rightarrow$ highest static friction.

[1]

$$\tan \theta = \mu_s \rightarrow \mu_s = \tan 45^\circ = 1$$

61)

Work $W = F \times dx$ because $t = \sqrt{x} + 3$
at $t = 6$ second.

$$dx = [x]_0^6$$

$$x = t^2 - 6t + 9$$

$$(x)_{t=0} \rightarrow 0^2 - 0 + 9 \rightarrow 9 \text{ m}$$

$$(x)_{t=6} \rightarrow 36 - 36 + 9 \rightarrow 9 \text{ m}$$

$$dx = 9 - 9 = 0 \checkmark$$

$$\text{Velocity } v = \frac{dx}{dt} = 2t - 6$$

$$\text{acceleration } a = \frac{dv}{dt} = 2$$

$$\text{Force } F = ma = 2m \checkmark$$

$$\therefore W = F \times dx = 2m \times 0 = 0 \text{ Joule.}$$

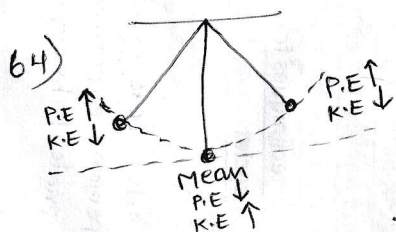
[2]

62) Power $P = \vec{F} \cdot \vec{v} = (5 \times 10) + (-3 \times 10) + (6 \times 20)$
 $= 50 - 30 + 120 = 140 \text{ watt}$

[3]

63) Solar Energy $\rightarrow$ Energy received by earth from SUN.
 $\rightarrow$ SUN (star) releases this energy with Nuclear Fusion of H, He

[2]



[2]

65) on the surface of earth $T_1 = 2\pi \sqrt{\frac{l}{g}}$

[4]

Above the surface of earth at a height R is.

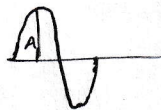
$$g' = g \left(\frac{R}{R+h}\right)^2 = g \left(\frac{R}{R+R}\right)^2 = \frac{g}{4} \downarrow$$

$$\therefore T_2 = 2\pi \sqrt{\frac{l}{g'}} = 2\pi \sqrt{\frac{4l}{g}}$$

$$T_2 = 2 \times 2\pi \sqrt{\frac{l}{g}} = 2T_1$$

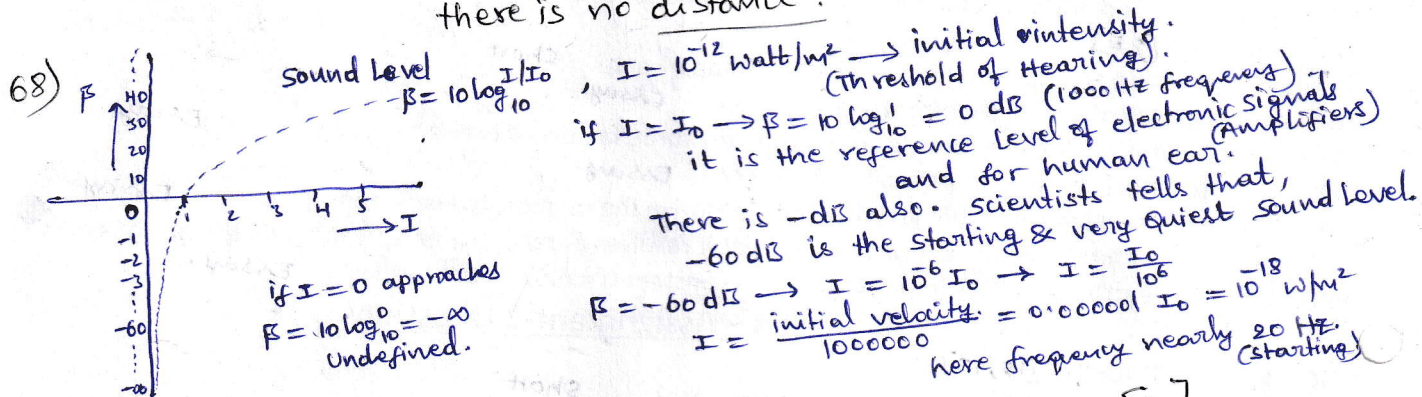
$$\frac{T_2}{T_1} = 2$$

- 66) Sound wave characteristics → Loudness → Amplitude
→ Intensity
→ Pitch → Frequency.
→ Quality → Remembrance (voice)



Wavelength → not a quantity for sound.

- 67) Doppler Effect $n' = \left(\frac{v \pm v_o}{v \pm v_s} \right) n$
 v_o → observer velocity
 v_s → source velocity
 n → Actual frequency → time also
 there is no distance.



69) $T_1 = 27 + 273 = 300 \text{ K}$

$V_2 = \frac{8}{27} V_1$

$\gamma = 5/3$

$T_2 = ?$

$TV^{\gamma-1} = \text{constant}$
 $T_1 V_1^{\gamma-1} = T_2 V_2^{\gamma-1}$
 $300 \times V_1^{\gamma-1} = T_2 \times \left(\frac{8V_1}{27} \right)^{\gamma-1}$
 $300 = T_2 \times \left(\frac{8}{27} \right)^{\frac{5}{3}-1}$

$300 = T_2 \left(\frac{2^3}{3^3} \right)^{\frac{2}{3}} = T_2 \times \left(\frac{2}{3} \right)^2$

$300 = T_2 \times \frac{4}{9} \rightarrow T_2 = 300 \times \frac{9}{4} = 675 \text{ K}$

rise in temperature $\Delta T = T_2 - T_1 = 675 - 300 = 375 \text{ K}$

70) $dQ = dU + dW$

$200 \text{ cal} = dU + 40 \text{ J} \rightarrow dU = (200 \times 4.2) - 40$
 $= 840 - 40$
 $dU = 800 \text{ Joule (+)} \rightarrow \text{increases.}$

71) $PV = nRT$

$P dv + v dp = nR dt$

$dW = nR dt + v dp$

$= nR dt + \frac{P}{\gamma} dt$

$= nR dt + \frac{PV}{T} dt$

$dW = nR dt + nR dt = 2nR dt$

$W = \int_T^{4T} 2nR dt = 2nR (T)^{4T}_T = 2nR (4T - T)$

$W = 6nRT$

72) isothermal $\rightarrow$ pressure $- P$
 volume $- V/4$
 Adiabatic $\rightarrow PV^{1.5} = \text{constant}$
 volume $- V/4$

$PV = \text{constant}$
 $PV = P_1 V_1 \rightarrow P_1 = \frac{PV}{V/4} = 4P$

$PV^{3/2} = P_2 V_2^{3/2}$
 $PV^{3/2} = P_2 \times \left(\frac{V}{4}\right)^{3/2}$
 $P = P_2 \times \frac{1}{2^3} \rightarrow P_2 = 8P$

[3]

$$\therefore \frac{P_2}{P_1} = \frac{8P}{4P} = 2$$

[2]

73) efficiency $\eta = 1 - \frac{T_c}{T_H} = 40\%$

$$1 - \frac{T_c}{500} = \frac{40}{100} \rightarrow \frac{T_c}{500} = \frac{60}{100} \rightarrow T_c = 300 \text{ K}$$

efficiency $\eta = 1 - \frac{T_c}{T_H} = 50\%$

$$1 - \frac{300}{T_H} = \frac{50}{100} = \frac{1}{2} \rightarrow \frac{300}{T_H} = 1 - \frac{1}{2} = \frac{1}{2}$$

$$\rightarrow T_H = 300 \times 2 = \underline{600 \text{ K}}$$